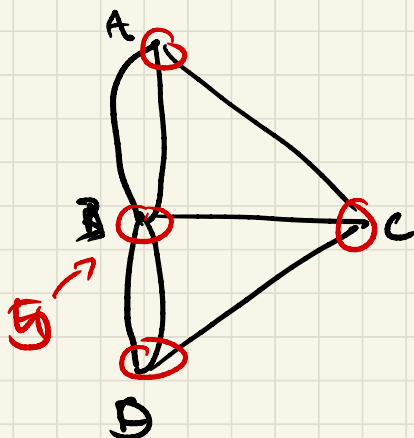


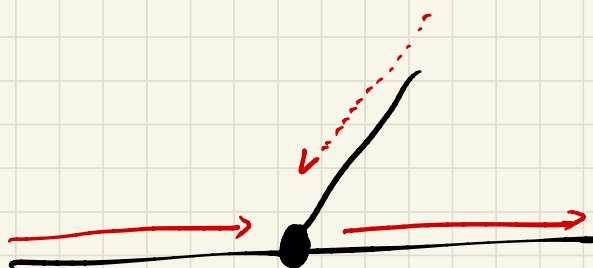
Not possible to  
do this walk!

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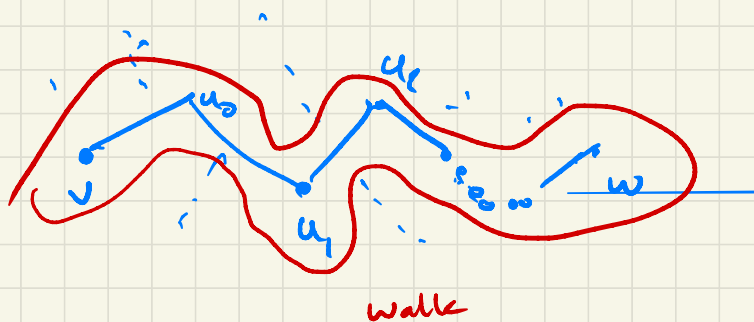
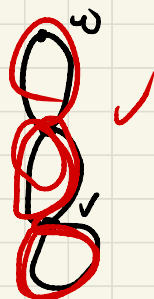
degree is  
always ~~even~~ odd



You get stuck!

Walk between  $v$  and  $w$

$v e u_0 e u_1 e u_2 e \dots e w$



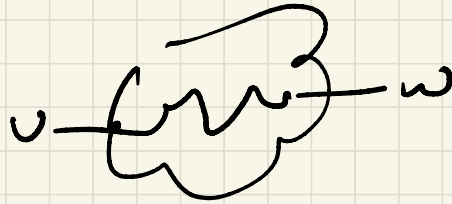
Trail



no  
repeated  
edges



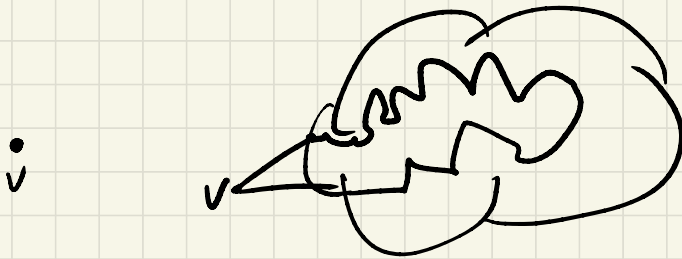
Path from  $v$  to  $w$



never repeat an edge

---

Closed walk



Comes back to where it starts!

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Circuit



Simple  
circuit

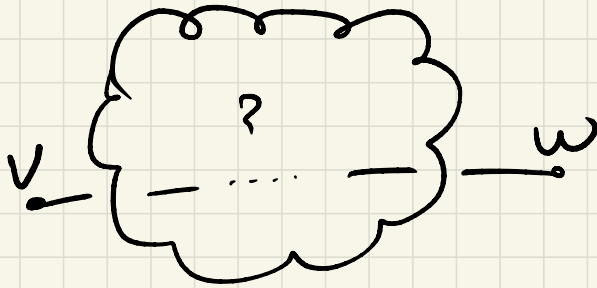
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Also no  
repeated  
vertices

---

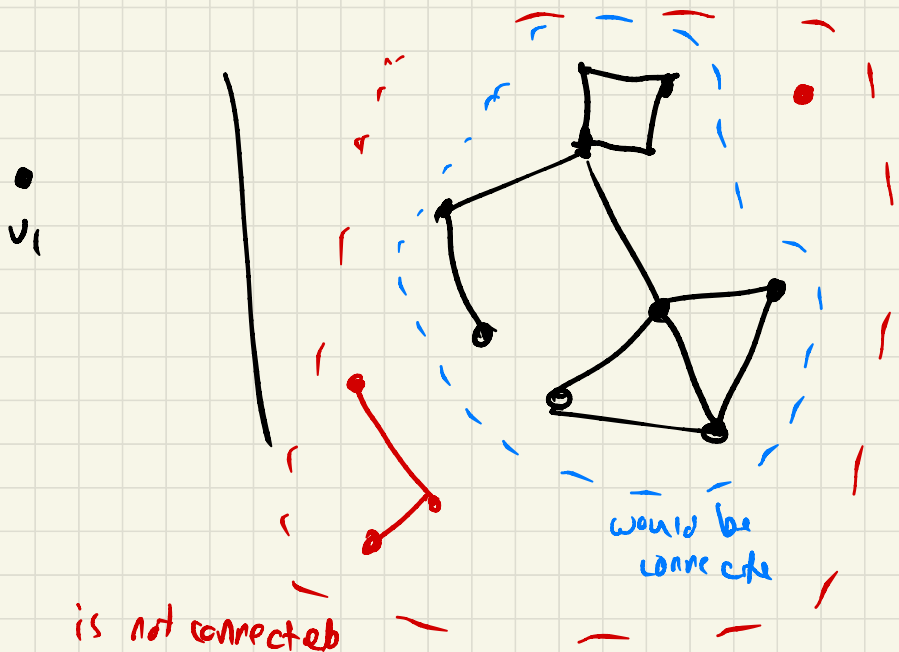
- Do not use an edge twice
- End up where you started

# Connectedness

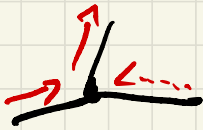


if so, we saw  $v$  and  $w$  are connected!

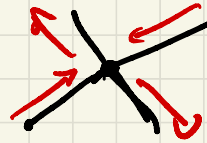
If every pair of vertices is  
connected, the graph is connected!



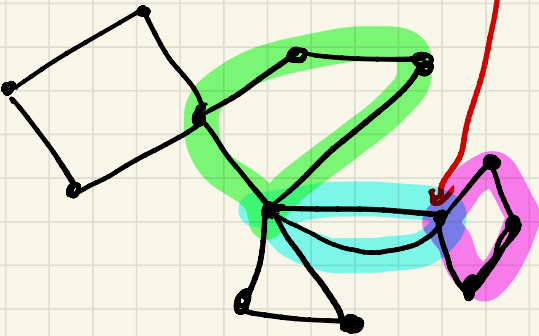
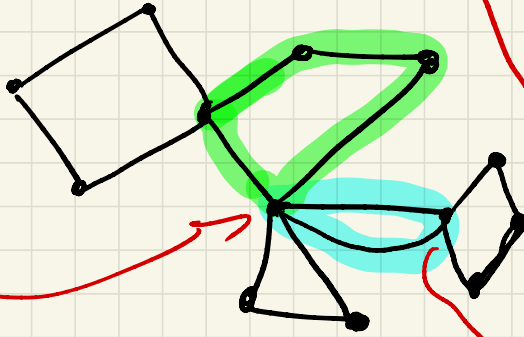
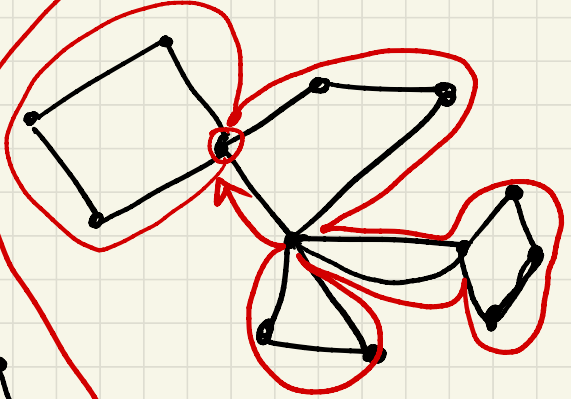
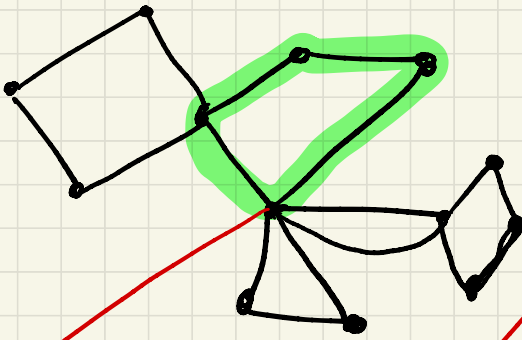
If all the degrees of the  
vertices in a graph are even  
then there exists an Euler  
circuit



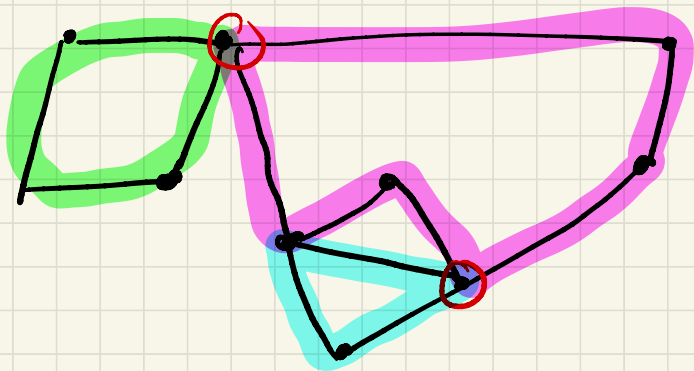
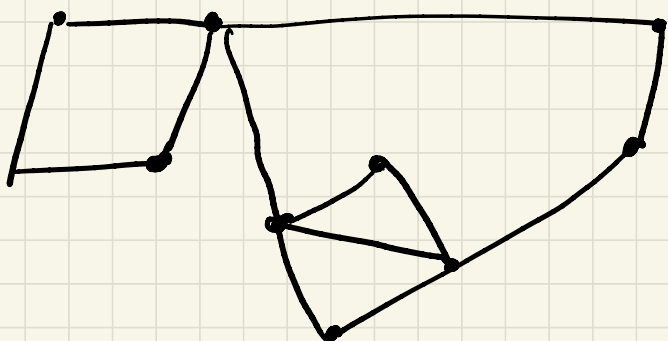
Your circuit  
gets stuck  
at odd vertices



You can't get  
stuck at even  
degree vertices!



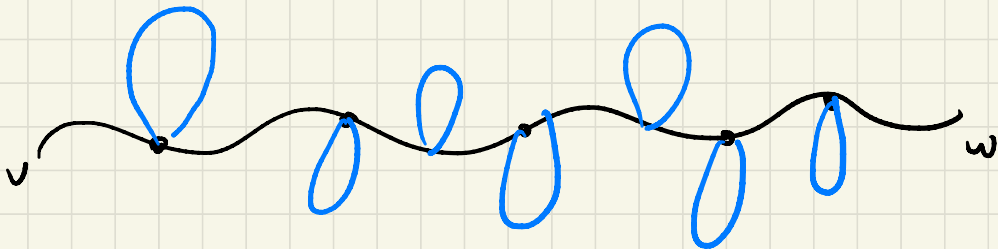
...





# Euler Trail

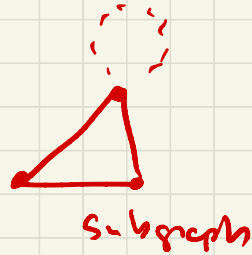
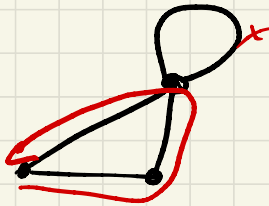
Like a Euler circuit  
but you start and end at  
different points.



Adding Euler circuits

# Hamilton Circuits

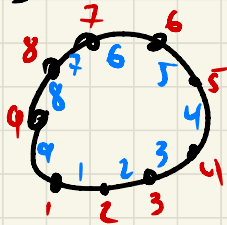
It must have a subgraph  $H$



It must be the case that  $H$   
contains vertices of  $G$

It must be connected.

$H$  must have the same number  
of edges



Every vertex of  $H$  has degree 2